



2011-2012
IB MYP YEAR 4

Signature

SUMMATIVE ASSESSMENT

Year 9 Mathematics (Extended)

Name: Jasmine Tuen [9 Hope] Ms. Li

Date of task: **8th June, 2012**

Time allowed: **1.5 hours (11:40 -13:10)**

Teacher: **Ms Li / Mr Millard / Mr So**

Student's Performance in Different Criteria			
A		C	

Instructions

- ◆ Read the instructions for all questions carefully.
- ◆ All work must be hand written.
- ◆ All work, steps and proper units must be shown.
- ◆ A non-electronic dictionary is allowed.
- ◆ Use of calculator is allowed.

Advice:

- ◆ Read the criteria descriptors and task-specific rubrics carefully before you start your work. This will give you a clear understanding of what is required and what a high quality piece of work for this task must include. This way you give yourself the best chance of achieving the highest levels in this task.
- ◆ This assessment task will be assessed on Criterion **A & C**.
 - ➡ For Criteria **A**, the questions are all assigned with levels;
 - ➡ Criterion **C** will be assessed as an overall impression on the presentation of work in this assessment.

ASSESSMENT CRITERIA

Criterion A: KNOWLEDGE AND UNDERSTANDING

Achievement level	Task Specific Rubric	IBO Published Descriptor
0	The student does not reach a standard described by any of the descriptors given below.	The student does not reach a standard described by any of the descriptors given below.
1–2 Simple	The student can solve <u>some</u> simple problems.	The student generally makes appropriate deductions when solving simple problems in familiar contexts.
3–4 Complex	The student can solve <u>most</u> simple and <u>some</u> more complex problems.	The student generally makes appropriate deductions when solving more complex problems in familiar contexts.
5–6 Challenging	The student can solve <u>some</u> challenging problem along with <u>all</u> different types of problems.	The student generally makes appropriate deductions when solving challenging problems in a variety of familiar contexts.
7–8 Unfamiliar	The student can solve <u>most</u> challenging and <u>most</u> unfamiliar problems along with <u>all</u> different types of problems.	The student consistently makes appropriate deductions when solving challenging problems in a variety of contexts including unfamiliar situations.

Criterion C: COMMUNICATION IN MATHEMATICS

Achievement level	Task Specific Rubric	IBO Published Descriptor
0	The student does not reach a standard described by any of the descriptors given below.	The student does not reach a standard described by any of the descriptors given below.
1–2	The student should be able to explain <u>some problems</u> step by step. The lines of reasoning are <u>difficult to follow</u> .	The student shows basic use of mathematical language and/or forms of mathematical representation. The lines of reasoning are difficult to follow .
3–4	The student should be able to explain <u>most problems</u> step by step. The lines of reasoning are <u>clear</u> though <u>not always</u> logical or <u>complete</u> .	The student shows sufficient use of mathematical language and forms of mathematical representation. The lines of reasoning are clear though not always logical or complete . The student moves between different forms of representation with some success .
5–6	The student should be able to explain <u>most problems</u> step by step. The lines of reasoning are concise, logical and complete . The student use correct unit in the questions.	The student shows good use of mathematical language and forms of mathematical representation. The lines of reasoning are concise, logical and complete . The student moves effectively between different forms of representation.

A. SIMPLE PROBLEMS

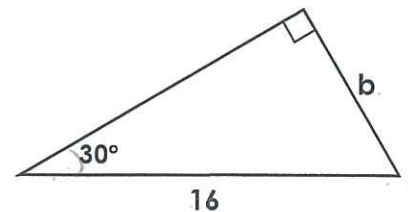
Suggested time allocation for Question 1 to 5 is **15 minutes**.

1. Given the points A $(-1, 2)$ and B $(2, k)$, find the value(s) of k such that the length of line AB is 5 units.

$$\begin{aligned}
 5 &= \sqrt{[2 - (-1)]^2 + (k - 2)^2} \\
 5 &= \sqrt{9 + k^2 + 4} \\
 5 &= \sqrt{k^2} \\
 5 - 3 &= k \\
 k &= -8
 \end{aligned}$$

2. In the figure on the right, find the value of b without using calculator.

$$\begin{aligned}
 \sin 30^\circ &= \frac{b}{16} \\
 \frac{1}{2} \times 16 &= b \\
 b &= 8
 \end{aligned}$$



3. Given that the equation of the line L_1 is $y - 2x = 4$, which of the following line(s) is/are **parallel to L_1** ? Which of the following line(s) has/have **negative y-intercepts**?

L2: $y = -2x + 4$

L3: $2y - 4x - 5 = 0$

L4: $-3y = 2x + 4$

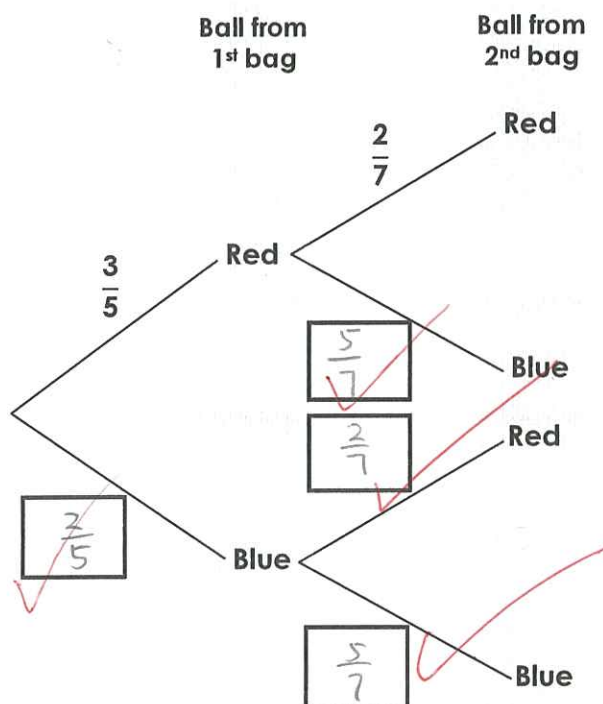
L5: $6x - 9 = 3y$

Explain your answers by showing your calculations.

$$\begin{aligned}
 L_1: -2x + 4 &= y \\
 y &= -2x + 4 \\
 L_2: y &= -2x + 4 \quad \checkmark \\
 \therefore L_2, L_3, L_5 &= -2x \\
 \therefore L_2, L_3, L_5 &\text{ are parallel with } L_1 \\
 L_3 \text{ is the line which have the negative } y\text{-intercepts}
 \end{aligned}$$

4. Loren has two bags. The **first** bag contains **3 red** balls and **2 blue** balls. The **second** bag contains **2 red** balls and **5 blue** balls. Loren takes **1 ball** at random from **each bag**.

(a) Complete the probability **tree diagram** by entering the **correct answers into the boxes**.



(b) Find the probability that Loren takes **two red balls**.

$$\frac{3}{5} \times \frac{2}{7} = \frac{6}{35} \quad P(\text{two red balls}) = \frac{6}{35}$$

5. Evaluate the following **without using calculator**.

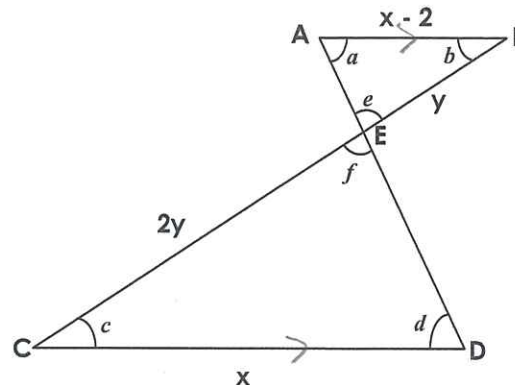
$$\sin^2 23^\circ + \cos^2 23^\circ - \frac{\sin 45^\circ}{\cos 45^\circ}$$

$$\begin{aligned} & \sin^2 23^\circ + \cos^2 23^\circ - \frac{\sin 45^\circ}{\cos 45^\circ} \\ &= 1 - \frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} \\ &= 1 - \frac{\sqrt{2}}{2} \times \frac{2}{\sqrt{2}} \\ &= 1 - \frac{\sqrt{2}}{2} \times \frac{2\sqrt{2}}{2} \\ &= 1 - \frac{2}{2} \\ &= 1 - 1 \\ &= 0 \end{aligned}$$

B. MORE COMPLEX PROBLEMS

Suggested time allocation for Question 6 to 9 is **25 minutes**.

6. In the figure below, the line AB is parallel to the line CD and some dimensions are shown in terms of x or y.



- (a) Show that $\triangle ABE$ and $\triangle DCE$ are **similar**. State the reason(s) if necessary.

In $\triangle ABE$ and $\triangle DCE$
 $\angle ABE = \angle ECD$ (alt \angle s $AB \parallel CD$)
 $\angle AEB = \angle CED$ (vert opp. \angle s)
 $\angle BAE = \angle CDE$ (\angle sum of Δ)
 $\therefore \triangle ABE \sim \triangle DCE$ (AAA)

- (b) Find the value of x.

In $\triangle ABE$ and $\triangle DCE$

$$\frac{AB}{DC} = \frac{BE}{CE} = \frac{AE}{DE}$$

$$\frac{x-2}{x} = \frac{y}{2y} = \frac{AE}{AD}$$

Let y be 2

$$\frac{x-2}{x} = \frac{2}{2(2)}$$

$$\frac{x-2}{x} = \frac{2}{4}$$

$$4x - 8 = 2x$$

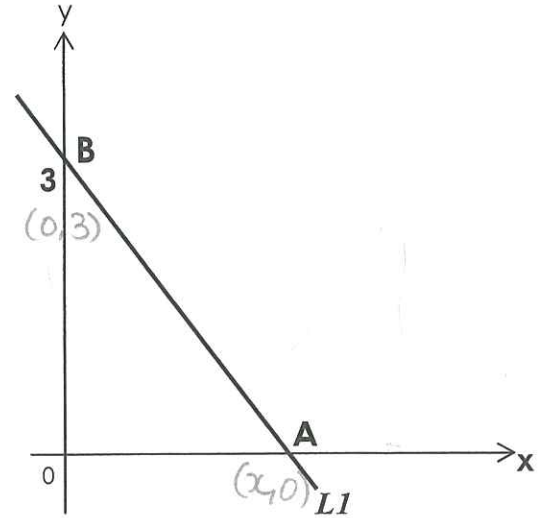
$$4x - 2x = 8$$

$$2x = 8$$

$$x = 4$$

7. In the graph on the right, a line $L1$ cuts the x-axis and y-axis at point **A** and **B** respectively. The y-intercept is 3.

- (a) If the area of the triangle AOB is 3 square units, find the **equation** of $L1$. Express your answer in **slope-intercept form**.



Let x be 2 why?

$$\frac{3-0}{0-2} = -\frac{3}{2}$$

$$-\frac{3}{2} = \frac{3-y}{2-x}$$

$$-6+3x = 6-2y$$

$$2y+3x-12=0$$

$$2y = -3x+12$$

$$y = -\frac{3}{2}x + \frac{12}{2}$$

$y = -\frac{3}{2}x + 6$

- (b) If a line $L2$ is **perpendicular** to $L1$ and two lines intersect at point **D(4,-3)**, find the equation of $L2$. Express your answer in **general form**.

$-\frac{3}{2} \times L2 = -1$ ✓

$-\frac{3}{2} \times L2 = 1$ ✓

$L2 = \frac{2}{3}$ ✓

$$\frac{2}{3} = \frac{y-(-3)}{x-4}$$

$$\frac{2}{3} = \frac{y+3}{x-4}$$

$$2x+4 = 3y+9$$

$$2x-3y-5 = 0$$

8. In a certain dice game, the player throws **two** typical unbiased **six-faces dice** and receives **\$5** if the sum is **7 or 11**, otherwise he or she **pays \$2**.

(a) Calculate the probability of obtaining the **sum of 7 or 11** when you throw the two dice once.

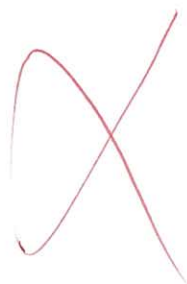
Dice 1 \ Dice 2	1	2	3	4	5	6
1		3	4	5	6	7
2	3	"	5	6	7	8
3	4	5		7	8	9
4	5	6	7		9	10
5	6	7	8	9		11
6	7	8	9	10	11	

$$P(7 \text{ or } 11) = \frac{1+3}{15}$$

$$= \frac{4}{15}$$

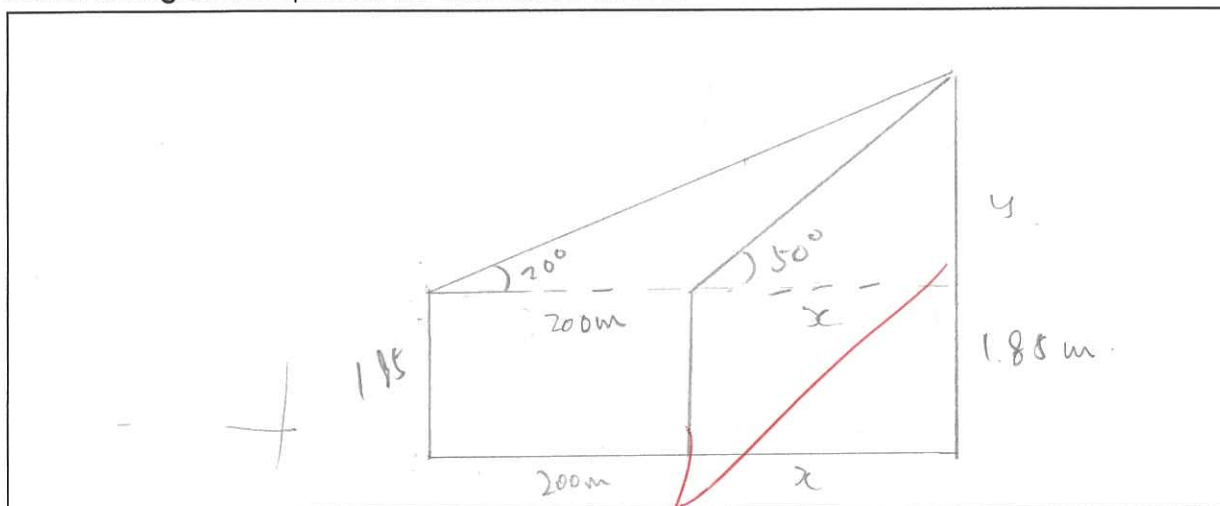


(b) If you play the game **18 times**, calculate the **amount of money** you expect to gain or lose.



9. Mr Bolivar, a volunteer fireman who is 1.85 m tall, is running towards a burning building where there is a fire on the roof. Initially, his angle of elevation to the roof is 20° . He runs for 200 m and now his angle of elevation is 50° . Assume that the ground is horizontal and the building is vertical.

(a) Sketch a **diagram** to represent the information above.



(b) How tall is the building? Correct your answer to the **nearest meter**.

$$\tan 20^\circ = \frac{1.85 + y}{200 + x}$$

let x be 0

$$\tan 20^\circ = \frac{1.85 + y}{200}$$

$$200 \times \tan 20^\circ = 1.85 + y$$

$$200 \times \tan 20^\circ - 1.85 = y$$

$$y = 70.9 \text{ m.}$$

$$70.9 + 1.85 = 72.75 \text{ m}$$

C. CHALLENGING PROBLEM

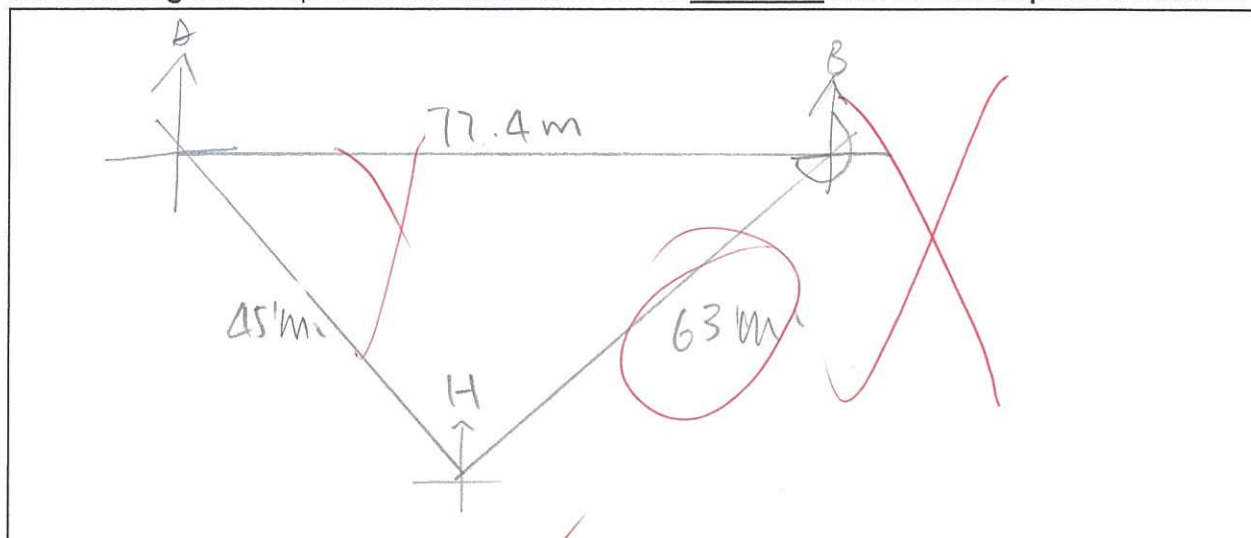
Suggested time allocation for Question 10 and 11 is **30 minutes**.

10. Ship **A** leaves the harbor **H** on a bearing **150°** with a speed of **40 km/hr**. At the same time, Ship **B** leaves harbor **H** on a bearing **210°** with a speed of **40 km/hr**.

- (a) **After 12 minutes**, how far did ship A and ship B travel?

$$A = \frac{150^\circ}{40 \times \frac{12}{60}} = 15 \times 3 = 45 \text{ m} \quad B = \frac{210^\circ}{40 \times \frac{12}{60}} = 63 \text{ m}$$

- (b) Sketch a **diagram** to represent the information above **12 minutes** after the two ships left the harbor.



- (c) Find the **true bearing** from Ship **A** to Ship **B** 12 minutes after they left the harbor.

$$180^\circ + 90^\circ = 270^\circ$$

- (d) Find the **distance between the two ships** 12 minutes after they left the harbor. Give your answer to the **nearest meter**.

$$\begin{aligned} AB &= \sqrt{45^2 + 63^2} \\ AB &= \sqrt{2025 + 3969} \\ &= \sqrt{5994} \\ &= 77.4 \text{ m} \end{aligned}$$

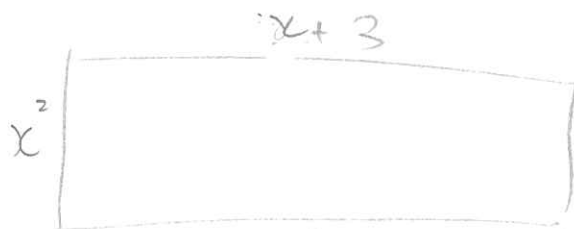
distance between 2 ships after 12 minutes they left the harbor is 77.4 m

11. The properties of a rectangle and a square are given below:

- ◆ The length of the rectangle is 3 cm longer than the side of the square.
- ◆ The width of the rectangle is double the length of the side of the square.

If the **sum of their areas** is **24 cm²**, find the **dimensions** (that is, its length and width) of the rectangle.

Let side of square



$$x^2 + x + 3$$

$$(x-1)(x-2)$$

D. Unfamiliar problems (Suggested time allocation for Question 12 and 13 is **30 minutes**.)

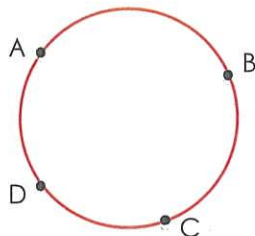
- 12.** At noon, Tom and Pete both park at the same starting point. Tom starts to ride his bike at 8 miles/hr. Two hours later, Pete starts after Tom on a bicycle at 12 miles/hr.

(a) How far will Tom have ridden before he is **overtaken by Pete**?

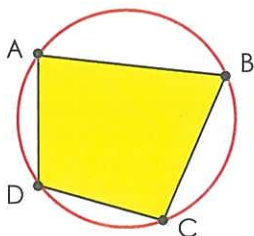
(b) At what time will Tom and Pete be **8 miles** apart?

13. Please read the following information and then do the proof on next page.

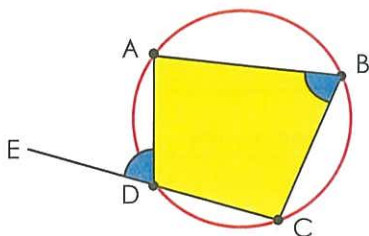
Points lie on the **same circle**, as the diagram below, are said to be **concyclic**. For example, A, B, C and D are **concyclic points**.



If the vertices of a **quadrilateral** lie on a **circle**, as the diagram below, then the quadrilateral is said to be **cyclic**. For example, ABCD is a **cyclic quadrilateral** since the vertices A, B, C and D lie on the circle.

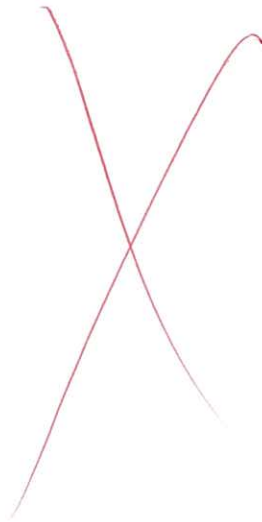
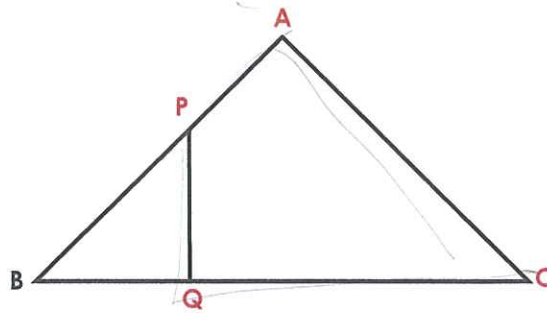


If the side CD is produced (i.e. extended) to E, as the diagram below, then $\angle ADE$ is called the **exterior angle of the cyclic quadrilateral ABCD**, and $\angle ABC$ is said to be the **interior opposite angle**.



Theorem: If $\angle ADE = \angle ABC$, then A, B, C and D are **concyclic**. (ext. \angle , int. opp. \angle)

In the figure below, $\triangle ABC$ and $\triangle BPQ$ are **isosceles** triangles such that $AB = AC$ and $BQ = PQ$. Using the provided information about the concyclic points and cyclic quadrilateral, **prove** that **A, P, Q and C are concyclic**.



End of Assessment

